

# FAIRNESS

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## MACHINE LEARNING HAS NO UNDERSTANDING

Machine learning creates black boxes that use probabilistic associations for prediction. It does not understand the causality that drives reality, and often struggles with uncertainty and bias.

# WE NEED FAIRNESS!

**FORTUNE** | EDUCATION  $\equiv$ 

NEWS B B C

What Zillow's failed algorithm means for the future of data science

February 01, 2022, 5:1



Big-data analysis told Zillow what to offer and how much to charge on the flip Easy peasy. Except, come 2021, the wheels came off. Zillow had bought thousands of houses, and the algorithms didn't factor in repairs with the skyrocketing costs

Twitter finds racial bias in image-cropping AI



Twitter's automatic cropping of images had underlying issues that favoured white individuals over black people, and women over men, the company said

# THE FAIR RIDGE REGRESSION MODEL (FRRM)

Consider a regression model with X predictors, S sensitive attributes, response y and a given level of fairness  $r \in [0, 1]$  (0 = complete fairness, 1 = no fairness constraints).

- 1. Compute  $\widehat{\mathbf{U}}$  (the fair predictors) as  $\mathbf{X} = \mathbf{S}\widehat{\mathbf{B}}_{\mathrm{OLS}} + \widehat{\mathbf{U}}$ .
- 2. Estimate  $\widehat{\boldsymbol{\beta}}_{\text{FRRM}} = \left(\widehat{\mathbf{U}}^{\text{T}}\widehat{\mathbf{U}}\right)^{-1}\widehat{\mathbf{U}}^{\text{T}}\mathbf{y}.$ 3. Estimate  $\widehat{\boldsymbol{\alpha}}_{\text{OLS}} = \left(\mathbf{S}^{\text{T}}\mathbf{S}\right)^{-1}\mathbf{S}^{\text{T}}\mathbf{y}$ .

Then:

- 4. If  $R^2_{\mathbf{S}}(\widehat{\boldsymbol{\alpha}}_{\mathrm{OLS}}, \widehat{\boldsymbol{\beta}}_{\mathrm{OLS}}) \leqslant r$ , set  $\widehat{\boldsymbol{\alpha}}_{\mathrm{FRRM}} = \widehat{\boldsymbol{\alpha}}_{\mathrm{OLS}}$ .
- 5. Otherwise, find the value of  $\lambda(r)$  that satisfies

$$R_{\mathbf{S}}^{2}(\boldsymbol{\alpha},\boldsymbol{\beta}) = \frac{\mathrm{VAR}(\mathbf{S}\boldsymbol{\alpha})}{\mathrm{VAR}(\mathbf{S}\boldsymbol{\alpha} + \widehat{\mathbf{U}}\widehat{\boldsymbol{\beta}}_{\mathrm{FRRM}})} = r$$

and estimate the associated  $\widehat{lpha}_{
m FRRM}$  in the process. FRRM solves  $\operatorname{argmin}_{\boldsymbol{\alpha},\boldsymbol{\beta}} \|\mathbf{y} - \mathbf{S}\boldsymbol{\alpha} - \widehat{\mathbf{U}}\boldsymbol{\beta}\|_2^2 + \lambda(r) \|\boldsymbol{\alpha}\|_2^2$ .



### **BBCNEWS**

Amazon scrapped 'sexist AI' tool

### () 10 October 2018



algorithm that was being tested as a recruitment tool by online giant Amazon was sexist and had to be scrapped, according to a Reuters report

### Documents show how data-driven policing programs reinforced harmful patterns, fueling the over-policing of **Black and brown communities**

programs amid public outcry. A new

LAPD ended predictive policing

effort shares many of their flaws

### WHAT WE WANT FROM FAIR MODELS

- Interpretability: What do the parameters mean in the domain the data come from?
- Explainability: Why does the model give specific predictions?
- Best practices: What are the best ways to select and validate models?
- **Confidence:** Are the effects we measure statistically significant? What is the error margin of predictions?

### **OPTIMISATION VS STATISTICS**

Optimisation approaches

Statistical approaches

- Single solution, computationally inexpensive.
- Pluggable fairness constraints.
- Works for all generalised linear models.
- Interpretable and explainable.
- ✓ A statistical model we know very well.

### **CONFIDENCE AND UNCERTAINTY**

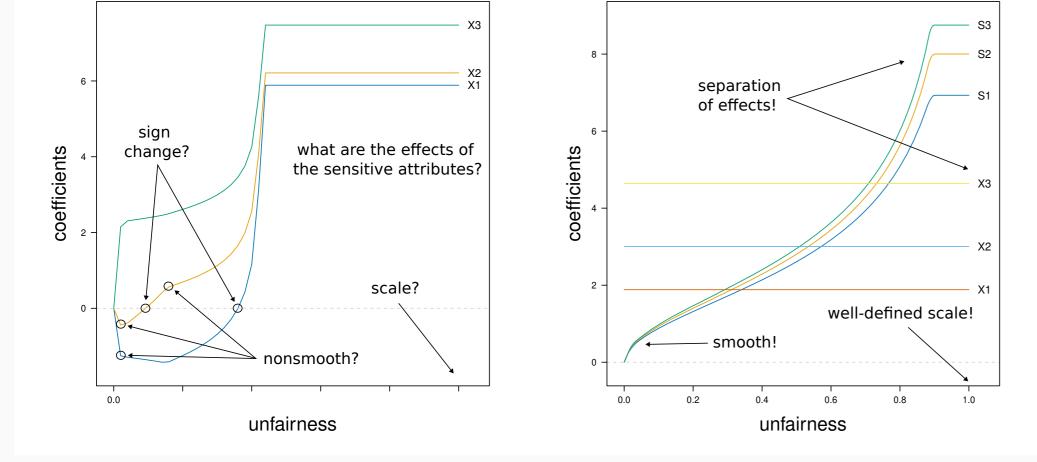
Bayesian statistics allows us to quantify uncertainty in our estimates in an easy and interpretable way. To design the Bayesian version of FRRM, we define the likelihood

$$\mathbf{y} \mid \boldsymbol{lpha}, \boldsymbol{eta}, \widehat{\mathbf{U}}, \mathbf{S} \sim \mathsf{MVN}\left(\widehat{\mathbf{U}} \boldsymbol{eta} + \mathbf{S} \boldsymbol{lpha}, rac{1}{ au} I
ight)$$

and the priors on  $\alpha, \beta$ , the penalty parameter  $\lambda$  and the precision  $\tau$ .

$$\begin{split} \boldsymbol{\beta} \mid \boldsymbol{\tau} \sim \mathsf{MVN} \left( \mathbf{0}, \frac{1}{\tau} I \right) \\ \boldsymbol{\alpha} \mid \boldsymbol{\tau}, \boldsymbol{\lambda} \sim \mathsf{MVN} \left( \mathbf{0}, \frac{1}{\tau \lambda} I \right) \\ \boldsymbol{\lambda} \sim \mathsf{Gamma} \left( \frac{1}{\tau^5} - 1, 1 \right) \\ \boldsymbol{\tau} \sim \mathsf{Gamma} \left( 1, 1 \right) \end{split}$$

Using this scheme, we can design a Gibbs sampler or Hamiltonian Monte Carlo algorithm to sample from the posterior of the parameters. This allows us to easily estimate the posterior distribution of the parameters and investigate their credible intervals.



### Posterior distribution and 90% credible intervals of alpha r = 0.1r = 0.1512r = 0.2r = 0.2510 r = 0.3---- OLS 8 Density 22alpha

### REFERENCES

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